

Living up to expectations

Estimating direct and indirect rebound effects for UK households

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SLRG Working Paper Series 15-01

ISSN: 2050 - 4446









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SLRG Working Paper 15-01

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Acknowledgements

The support of the Department for Environment, Food and Rural Affairs (Defra), the Economic and Social Research Council (ESRC) and the Scottish Government is gratefully acknowledged. This work is part of the research programme of SLRG - the Sustainable Lifestyles Research Group.

ISSN: 2050-4446

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Abstract

This study estimates the combined direct and indirect rebound effects from various types of energy efficiency improvement by UK households. In contrast to most studies of this topic, we base our estimates on cross-price elasticities and therefore capture both the income and substitution effects of energy efficiency improvements. Our approach involves estimating a household demand model to obtain price and expenditure elasticities of different goods and services, utilising a multiregional input-output model to estimate the GHG emission intensities of those goods and services, combining the two to estimate direct and indirect rebound effects, and decomposing those effects to reveal the relative contribution of different mechanisms and commodities. We estimate that the total rebound effects are 63% for measures that improve the efficiency of domestic gas use, 53% for electricity use and 46% for vehicle fuel use. The primary source of this rebound is increased consumption of the cheaper energy service (i.e. direct rebound) and this is primarily driven by substitution effects. Our results suggest that the neglect of substitution effects may have led prior research to underestimate the total rebound effect. However, we provide a number of caveats to this conclusion, as well as indicating priorities for future research.

Keywords: Rebound effects; Income and substitution effects; linear almost ideal demand system

1 Introduction

'Rebound effects' is a widely used term for a variety of economic responses to improved energy efficiency. The net result of these effects is typically to increase energy consumption and greenhouse gas (GHG) emissions relative to a counterfactual baseline in which these responses do not occur. To the extent that rebound effects are neglected in policy appraisals, the energy and emissions 'saved' by such measures may be less than anticipated.

Studies of rebound effects for consumers typically focus upon the *direct* effects that result from increased consumption of cheaper energy services. For example, fuel-efficient cars make driving cheaper so people may drive further and/or more often (Small and Van Dender, 2007; Sorrell, 2007). But a comprehensive accounting of the global environmental impact of energy efficiency improvements must also take into account various *indirect* rebound effects. For example, any savings on petrol bills may be put towards increased consumption of other goods and services whose provision also involves energy use and emissions at different stages of their global supply chains (Chitnis et al., 2013; Druckman et al., 2011b). To quantify indirect rebound effects, it is necessary to combine econometric analysis of household (re)spending patterns with estimates of the energy and emissions 'embodied' within different categories of goods and services. The latter, in turn can be derived from environmentally extended, multiregional input-output models (Druckman and Jackson, 2009; Turner et al., 2007; Wiedmann et al., 2007).

Relatively few studies estimate both direct and indirect rebound effects and most of these rely upon expenditure elasticities rather than cross-price elasticities. As a result, they capture the *income* effects of energy efficiency improvements but not the *substitution* effects (Chitnis et al., 2014). To appreciate the distinction, consider a household that installs insulation and

recovers the capital costs over ten years through lower heating bills. Since the bill savings exactly offset the capital costs, there is no increase in real income over this period so the income effect is zero. Hence, studies that focus solely upon income effects would estimate the direct and indirect rebound effects over that period to be zero as well. But since the unit cost of heating has fallen relative to that of other goods and services, the household is likely to consume more heating and fewer goods and services that are 'substitutes' to heating. At the same time, the household may consume more of other goods and services that are 'complements' to heating. The net result will be a shift in consumption patterns and hence a change in the GHG emissions associated with that consumption that may offset the original emission savings. Hence, it is possible that studies that neglect substitution will underestimate rebound effects.

This study therefore addresses the limitations of the existing literature by: a) estimating the magnitude of both direct and indirect rebound effects following the adoption of energy efficiency measures by households; b) identifying the relative contribution of income and substitution effects to these results; and c) identifying the relative contribution of individual goods and services. This is the first study to estimate these effects for UK households, as well as the first to decompose them to this level of detail.

The paper is structured as follows. Section 2 introduces the relevant concepts, highlights some methodological trade-offs and summarises the existing literature. Section 3 outlines the methodology, including the data sources used, the economic model adopted and the econometric techniques employed. Section 4 presents the results, including the estimates of direct and indirect rebound effects and the contribution of different mechanisms and commodities to those effects. Section 5 discusses the robustness of the results and highlights some implications. Section 6 concludes.

2 Concepts and previous work

2.1 Direct rebound effects

Cost-effective energy efficiency improvements reduce the effective price of energy services such as heating and lighting, thereby encouraging increased consumption of those services that offsets the initial energy and emission savings. The marginal change in the energy (q_e) required to provide a given quantity of energy service (q_s) following a marginal change in energy efficiency ($\varepsilon = q_s/q_e$) may be expressed as:

$$\eta_{q_e,\varepsilon} = \frac{\partial \ln q_e}{\partial \ln \varepsilon}$$

As shown by Sorrell and Dimitropoulos (2007a), this may be written as:¹

$$\eta_{q_e,\varepsilon} = -\eta_{q_s,p_s} - 1$$

Where η_{q_s,p_s} is the own-price elasticity of demand for the energy service (q_s) with respect to the energy cost of that service $(p_s = p_e / \varepsilon)$. The negative of this elasticity is commonly taken as a measure of the *direct rebound effect* (R_D) (Sorrell and Dimitropoulos, 2007a):

$$R_D = -\eta_{q_s, p_s}$$

¹ Given $q_e = q_s / \varepsilon$, $q_s = f(p_s)$ and $p_s = p_e / \varepsilon$, we have: $\eta_{q_e,\varepsilon} = \frac{\partial q_e}{\partial \varepsilon} \frac{\varepsilon}{q_e} = \frac{\varepsilon}{q_e} \left[-\frac{q_s}{\varepsilon^2} + \frac{\partial q_s}{\partial p_s} \frac{\partial p_s}{\partial \varepsilon} \right]$ Or: $\eta_{q_e,\varepsilon} = \frac{\varepsilon}{q_e} \left[-\frac{q_s}{\varepsilon^2} - \frac{1}{\varepsilon} \frac{p_e}{\varepsilon^2} \frac{\partial q_s}{\partial p_s} \right] = \frac{q_s}{\varepsilon q_e} - \frac{p_e}{\varepsilon^2 q_e} \frac{\partial q_s}{\partial p_s} = -1 - \frac{p_s}{q_s} \frac{\partial q_s}{\partial p_s}$. So: $\eta_{q_e,\varepsilon} = -\eta_{q_s,p_s} - 1$ If the energy service is a normal good $(0 \ge \eta_{q_s, p_s})$ there will be a positive direct rebound effect $(R_D \ge 0)$. This may be decomposed into a *substitution* effect and an *income* effect² using the Slutsky equation:

$$\eta_{q_s, p_s} = \tilde{\eta}_{q_s, p_s} - w_s \eta_{q_s, x} \tag{4}$$

Where: w_s is the share of the energy service in total household expenditure (x); $\eta_{q_s,x}$ is the expenditure elasticity of the energy service; and $\tilde{\eta}_{q_s,p_s}$ is the *compensated* own-price elasticity of demand for the energy service, holding utility (u) constant:

$$w_s = \frac{p_s q_s}{x}; \ \eta_{q_s, x} = \frac{\partial \ln q_s}{\partial \ln x}; \text{ and } \ \widetilde{\eta}_{q_s, p_s} = \frac{\partial \ln q_s}{\partial \ln p_s} \bigg|_{u=constant}$$
5

In Equation 4, $\tilde{\eta}_{q_s,p_s}$ measures the substitution effect while $-w_s\eta_{q_s,x}$ measures the income effect. These may offset or reinforce one another. Table 1 summarises the influence of these terms on the sign of the direct rebound effect.

² The former is the change in consumption that would result from the change in relative prices if real income were adjusted to keep utility constant, while the latter is the change in consumption that would result exclusively from this change in real income.

Nature	Sign of	Sign of	Relative size of	Sign of	Sign of
of	expenditure	compensated	income and	uncompensated	direct
energy	elasticity	own-price	substitution	own-price	rebound
service		elasticity	effects	elasticity	effect
Normal	$\eta_{q_s,x} > 0$	$\widetilde{\eta}_{q_s,p_s} < 0$	Not relevant	$\eta_{q_s,p_s} < 0$	$R_D > 0$
good					
Inferior	$\eta_{q_s,x} < 0$	${\widetilde \eta}_{q_s,p_s} < 0$	$\left \widetilde{\eta}_{q_s, p_s} \right > \left w_s \eta_{q_s, x} \right $	$\eta_{q_s,p_s} < 0$	$R_D > 0$
good					
Giffen	$\eta_{q_s,x} < 0$	$\widetilde{\eta}_{q_s,p_s} < 0$	$\left \widetilde{\eta}_{q_s,p_s}\right < \left w_s \eta_{q_s,x}\right $	$\eta_{q_s,p_s} > 0$	$R_D < 0$
good					

Table 1 Determinants of the sign of the direct rebound effect

2.2 Indirect rebound effects

Energy efficiency improvements may also change the quantity demanded of other goods and services. These include both other energy services (e.g. heating) and other non-energy goods and services (e.g. furniture) that 'embody' the energy and emissions required to manufacture, transport and deliver them. These changes in consumption patterns will impact energy use and emissions at each stage of the relevant supply chains. From a global perspective, these changes may either offset or add to the energy and emission savings from the energy efficiency improvement depending on whether the quantity demanded of the relevant goods or service has increased or fallen. The *indirect rebound effect* (R_{I_i}) from an individual commodity (*i*) will be proportional to this change in energy and emissions, which in turn will depend upon: the energy or emissions intensity of the commodity relative to that of the

energy service; and the elasticity of demand for the commodity with respect to the price of the energy service. The latter is defined as:

$$\eta_{q_j, p_s} = \frac{\partial \ln q_i}{\partial \ln p_s} \tag{6}$$

Again, this elasticity can be decomposed:

$$\eta_{q_i, p_s} = \tilde{\eta}_{q_i, p_s} - w_s \eta_{q_i, x}$$

Where: w_s is the share of the energy service in total household expenditure; $\eta_{q_i,x}$ is the expenditure elasticity of commodity *i*; and $\tilde{\eta}_{q_i,p_s}$ is the compensated elasticity of demand for commodity *i* with respect to the energy cost of the energy service:

$$w_s = \frac{p_s q_s}{x}; \ \eta_{q_i,x} = \frac{\partial \ln q_i}{\partial \ln x}; \text{ and } \ \widetilde{\eta}_{q_i,p_s} = \frac{\partial \ln q_i}{\partial \ln p_s}\Big|_{u=constant}$$
 8

Again, the substitution effect for commodity i ($\tilde{\eta}_{q_i, p_s}$) may offset or reinforce the income effect ($-w_s \eta_{q_i, x}$). Table 2 summarises the influence of these terms on the sign of the indirect rebound effect associated with commodity *i*. Commodities that are gross complements (substitutes) to the energy service will contribute a positive (negative) indirect rebound effect, with the overall effect being given by the sum of these over all commodities ($R_I = \sum_i R_{I_i}$).

Nature of	Sign of	Sign of	Relative size of	Sign of	Sign of
commodity	expenditure	compensated	income and	uncompensated	indirect
i	elasticity	cross-price	substitution effects	cross-price	rebound
	for	elasticity		elasticity	effect for
	commodity				commodity
	i				i
Normal	$\eta_{q_i,x} > 0$	$\tilde{\eta}_{q_i,p_s} < 0$	Not relevant	$\eta_{q_i,p_s} < 0$	$R_{I_i} > 0$
good		Net		Gross	
		complements		complements	
Normal	$\eta_{q_i,x} > 0$	$\widetilde{\eta}_{q_i,p_s} > 0$	$\left \widetilde{\eta}_{q_i, p_s} \right < \left w_s \eta_{q_i, x} \right $	$\eta_{q_i,p_s} < 0$	$R_{I_i} > 0$
good		Net substitutes		Gross	
				complements	
Normal	$\eta_{q_i,x} > 0$	$\widetilde{\eta}_{q_i,p_s} > 0$	$\left \widetilde{\eta}_{q_i, p_s} \right > \left w_s \eta_{q_i, x} \right $	$\eta_{q_i,p_s} > 0$	$R_{I_i} < 0$
good		Net substitutes	11.1 3	Gross substitutes	
Inferior	$\eta_{q_i,x} < 0$	$\widetilde{\eta}_{q_i,p_s} < 0$	$\left \widetilde{\eta}_{q_i, p_s} \right > \left w_s \eta_{q_i, x} \right $	$\eta_{q_i,p_s} < 0$	$R_{I_i} > 0$
good		Net		Gross	
		complements		complements	
Inferior	$\eta_{q_i,x} < 0$	$\widetilde{\eta}_{q_i,p_s} < 0$	$\left \widetilde{\eta}_{q_i, p_s} \right < \left w_s \eta_{q_i, x} \right $	$\eta_{q_i,p_s} > 0$	$R_{I_i} < 0$
good		Net	1 11 / 1 3 '	Gross substitutes	
		complements			
Inferior	$\eta_{q_i,x} \leq 0$	$\widetilde{\eta}_{q_i,p_s} > 0$	Not relevant	$\eta_{q_i,p_s} > 0$	$R_{I_i} < 0$
good		Net substitutes		Gross substitutes	

Table 2 Determinants of the sign of the indirect rebound effect for commodity j

2.3 Trade-offs in estimating direct and indirect rebound effects

To estimate direct and indirect rebound effects we need the own- and cross-price elasticities for the relevant energy service. This requires the estimation of a *household demand model* namely, a system of n equations representing household demand for n commodities as a function of total expenditure, commodity prices and other variables, with one of these commodities being the energy service (s).

A growing number of studies estimate own-price elasticities for individual energy services (η_{q_i,p_s}) , but to our knowledge no study has estimated cross price elasticities (η_{q_i,p_s}) owing the difficulties of specifying energy services as a 'commodity' within a household demand model (Sorrell, 2010). Since energy services are produced from a combination of energy commodities (e.g. gas) and durable goods (e.g. boilers), specifying their energy cost (p_s) and quantity demanded (q_s) involves combining data on energy commodity purchases with additional data on the ownership and energy efficiency of the relevant durables (Conrad and Schröder, 1991). Since this data may not be available, a simpler alternative is to estimate a model for purchased commodities (i) and to simulate energy efficiency improvements by a reduction in the price of the relevant energy commodities (l) (e.g. 2007). So, for example, more efficient boilers may be simulated by a reduction in the unit price of natural gas (p_l) , since both will reduce the energy cost of heating (p_s) . Elasticities may then be estimated with respect to energy commodity prices (p_l) , rather than energy service prices (p_s) and used to estimate both direct and indirect rebound effects. This approach is simpler to implement but, as discussed below, may potentially lead to biased estimates of rebound effects.

It is common to formulate household demand models in terms of expenditures (x_i) rather than quantity demanded (q_i) since expenditures are easier to measure. The following relationships may be derived:

$$\eta_{x_i, p_i} = 1 + \eta_{q_i, p_i}; \quad \tilde{\eta}_{x_i, p_i} = 1 + \tilde{\eta}_{q_i, p_j}; \quad 9$$

$$\eta_{x_i,p_j} = \eta_{q_i,p_j}; \quad \tilde{\eta}_{x_i,p_j} = \tilde{\eta}_{q_i,p_j}$$
10

$$\eta_{x_i,x} = \eta_{q_i,x} \tag{11}$$

Household demand models can be estimated from pooled cross-sectional data on household expenditures and commodity prices. But the number of coefficients to be estimated limits the degrees of freedom³, with the result that expenditures need to be aggregated into a limited number of commodity groups. For the same reason, such models provide limited scope for including covariates and typically require restrictions to be imposed upon the parameter values to increase the degrees of freedom. A common strategy is to assume *separability* of preferences between aggregate commodity groups such as food and transport, implying that decisions on how much to spend on one group (e.g. transport) are separate from decisions on how to allocate this expenditure between the goods and services within that group (e.g. bus,

³ For example, suppose the demand equations took the form: $\ln q_i = \alpha_i + \eta_i \ln x + \sum_{j=1,n} \varepsilon_{ij} \ln p_j$; where is η_i is the expenditure elasticity for commodity *i* and ε_{ij} are the price elasticities. In this system of *n* equations there are *n* intercepts ($\alpha_1, \alpha_2, ..., \alpha_n$), *n* expenditure elasticities ($\eta_1, \eta_2, ..., \eta_n$) and n^2 price elasticities (ε_{ij} *i*, *j* = 1,...*n*), leading to a total of *n*(2+*n*) coefficients. So for example, if there were ten commodity groups (*n*=10) there would be 120 coefficients to estimate, implying the need for long time series.

car or train travel) (Deaton and Muellbaeur, 1980).⁴ This is a restrictive assumption, but it can work reasonably well if the categories are well chosen

An alternative approach is to use cross-sectional data on household expenditure to estimate *Engel curves* for each commodity group – indicating how expenditure on each commodity varies with total expenditure (Deaton and Muellbaeur, 1980). Engel curves allow expenditure elasticities to be estimated but not price elasticities - since the data provides no variation in commodity prices. As a result, they only allow the income effects of energy efficiency improvements to be estimated and not the substitution effects. However, Engel curves are simpler to estimate than full household demand models and permit the disaggregation of household expenditure into a larger number of commodity groups. Since there are typically more degrees of freedom, they also make it easier to include covariates and require fewer restrictions. The choice of methodological approach therefore involves some trade-offs and will depend upon the objectives of the study (Sorrell, 2010). We estimate a full household demand model in what follows, because we are particularly interested in the relative size of income and substitution effects.

2.4 Previous work

Tables 3 and 4 classify the limited number of studies that estimate both direct and indirect rebound effects for households - with those in Table 3 using expenditure elasticities (income effects) and those in Table 4 using cross-price elasticities (income and substitution effects). While most studies focus upon improved energy efficiency in electricity, heating or car

⁴ 'Weak separability' implies that the marginal rate of substitution between commodities in one group is independent of the quantities of other commodities in other groups. This allows the demand for commodities within a group to be written solely as a function of the expenditure on the group and the prices of commodities within the group, with the prices of other commodities only affecting the group expenditure and not the allocation of expenditure within the group.

travel, others examine 'sufficiency' measures such as reducing car travel or food waste.⁵ Different studies estimate rebound effects in energy, carbon and GHG terms, but no study estimates and compares all three. This diversity, combined with the methodological limitations of each study (Sorrell, 2010) makes it difficult to draw robust conclusions.

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⁵ Since sufficiency measures do not change the effective price of the energy service, there are no associated substitution effects.

Author	Region	No. of commodity	Measure	Area	Metric	Energy/	Estimated rebound
		categories				emissions	effect (%)
Lenzen and Day	Australia	150	Efficiency &	Food; heating	GHGs	Direct and	45-123%
(2002)			sufficiency			embodied	
Alfreddson	Sweden	300	Sufficiency	Food; travel; utilities	CO ₂	Direct and	7-300%
(2004)						embodied	
Druckman et al	UK	16	Sufficiency	Transport, heating,	GHGs	Direct and	7-51%
(2011a)				food		embodied	
Thomas and	US	13	Efficiency	Transport, electricity	Energy and	Direct and	7-25%
Azevedo					CO_2	embodied	
(2013)							
Murray	Australia	36	Efficiency &	Transport, lighting	GHGs	Direct and	4-24%
(2013)			sufficiency			embodied	
Chitnis et al	UK	16	Efficiency	Heating, lighting	GHGs	Direct and	5-15%
(2013)						embodied	
Chitnis et al	UK	16	Efficiency and	Transport, heating,	GHGs	Direct and	5-106%
(2014)			sufficiency	lighting, food		embodied	

Table 3: Studies estimating combined direct and indirect rebound effects for households –income effects only

Author	Region	No. of commodity	Measure	Area	Metric	Energy/	Estimated rebound
		categories				emissions	effect (%)
Brannlund et al	Sweden	13	Efficiency	Transport; utilities	CO ₂	Direct and	120-175%
(2007)						embodied	
Mizobuchi (2008)	Japan	13	Efficiency	Transport; utilities	CO ₂	Direct and	12-38%
						embodied	
Lin et al (2013)	China	10	Efficiency	Transport; utilities	CO ₂	Direct and	37%
						embodied	
Kratena and Wuger	Austria	6	Efficiency	Transport; heating;	Energy	Direct only	37-86%
(2008)				electricity			

Table 4: Studies estimating combined direct and indirect rebound effects for households – income and substitution effects

Brannlund *et al* (2007) was the first study to use cross-price elasticities to estimate combined direct and indirect rebound effects. Using survey data for Swedish households over the period 1980-1997, Brannlund *et al* estimate a household demand model⁶ for 13 categories of nondurable expenditure. Separability assumptions are used to: first, allocate expenditure between durables and non-durables; second, allocate non-durable expenditure between four aggregate groups (food, transport, domestic energy and other); and third, distribute the group expenditures between individual commodities within each group (e.g. domestic energy is subdivided into oil, electricity and district heating). Brannlund *et al* then simulate a 20% energy efficiency improvement in transport and domestic energy by reducing the price of each commodity in proportion to the estimated contribution of energy to total costs, and then recalculate the model to estimate the impact on global carbon emissions. The results suggest a rebound effect of 121% for transport efficiency improvements, 175% for domestic energy and 140% for both combined.⁷

Brannlund *et al* do not separately investigate efficiency improvements in electricity and heating fuels, do not distinguish between direct and embodied emissions and do not calculate the relative contribution of income and substitution effects to their results - despite estimating the relevant elasticities. More importantly, their estimated rebound effects are remarkably large and suggest that direct rebound effects *alone* exceed 100%. This contradicts the results of a growing body of work that estimates direct rebound effects for these energy services in OECD households (Sorrell et al., 2009), together with a larger body of work that estimates the corresponding energy price elasticities (Sorrell and Dimitropoulos, 2007b).

⁶ All three of the studies described here estimate the linear *Linear Almost Ideal Demand System (LAIDS)* introduced by Deaton and Muellbauer (1980).

⁷ The presentation of results is misleading. For example, transport efficiency is estimated to reduce carbon emissions by 6.2% in the absence of rebound effects but to increase carbon emissions by 1.3% once rebound effects are accounted for. Brannlund *et al.* report this as a rebound effect of 7.5%, whereas the correct value is 121%.

Mizobuchi (2008) takes a similar approach to Brannlund *et al*, using monthly expenditure data for Japanese households over the period 1990-98.⁸ He also employs multistage budgeting, but in contrast to Brännlund *et al*, the 13 commodities represent expenditure on both durables and non-durables (e.g. both cars and road fuel) and hence cover all household emissions. Mizobuchi simulates simultaneous reductions in the price of domestic energy and road fuels, but the percentage improvements are different from those in Brannlund *et al* and vary from one commodity to another. Two scenarios are investigated: one where the efficiency improvements are costless, and a second where adjustments are made to reflect the additional capital cost of energy-efficient equipment.⁹ This leads to an estimated rebound effect of 115% in the first scenario (similar to Brannlund *et al*) and 27% in the second.

Mizobuchi argues that allowing for capital costs reduces the cost savings and hence the estimated rebound effects. But the manner in which this scenario is implemented also changes the *relative* cost savings between electricity, gas, heating oil and vehicle fuels, leading to substitution between them that modifies the estimated rebound effects. Since Mizobuchi does not report the rebound effects for each individual efficiency improvement, the drivers of the results are obscured.

Lin and Liu (2013) also follow Brannlund *et al*'s approach, using annual data for Chinese urban households over the period 1986-2007. Their focus is a 30% improvement in energy efficiency for transport and domestic energy, but the assumed price reductions in each

⁸ Methodological innovations include Bayesian estimation methods and the use of an iterative procedure to estimate rebound effects.

⁹ Mizobuchi assumes 20% improvement in the efficiency of electricity and road fuel use, 10% in gas use and 3% in heating oil use. Achieving these is assumed to require a 22% increase in expenditure on durables for electricity, 35% for gas, 12% for heating oil and 28% for vehicles. The final percentage change in the price of the relevant subcategory (e.g. car transport) then depends upon the relative proportion of durable and nondurable expenditure within that category. The method of calculating additional capital costs is crude and leads, for example, to the odd result that fuel-efficient cars are more expensive than inefficient cars. This is because newer and more fuel-efficient cars of a particular model type are more expensive than older and less efficient cars of the same type. But this neglects the differences in cost and fuel efficiency *between* model types in the same year and between different sizes of vehicle.

subcategory are not specified. They estimate a total rebound effect of 37%, of which 12.6% is direct and 24.4% indirect.¹⁰ But they do not separately estimate the rebound effects for transport and domestic energy, and do not specify the relative contribution of income and substitution effects to their results.

Finally, Kratena and Wuger (2008) provide only a partial picture since they confine attention to a subset of commodity groups and neglect embodied emissions. They find large rebound effects (37-86%), but this study has not been peer-reviewed and has a number of weaknesses (Sorrell, 2010).

In sum, the existing evidence base is limited and inadequately explained. The estimated rebound effects from both the Brannlund and Mizobuchi studies appear larger than those in Table 3 and inconsistent with the growing literature on direct rebound effects. Also, none of the studies in Table 4 clarify the relative contribution of income and substitution effects to their results, or the relative contribution of direct and embodied emissions. Our analysis addresses these limitations.

3 Methodology

Our approach involves estimating a household demand model to derive price and expenditure elasticities of different goods and services, utilising a multiregional input-output model to estimate the GHG emission intensities of those goods and services, combining the two to estimate direct and indirect rebound effects, and decomposing those effects to reveal the relative contribution of different mechanisms and commodities. Section 3.1 develops

¹⁰ The numbers in the summary and abstract of Lin and Liu (2013) are incorrect, while those in the body of the paper are correct.

analytical expressions for these effects, Section 3.2 describes the econometric model and Section 3.3 summarises the data.

3.1 Rebound model

Assume a household makes a costless investment that increases the energy efficiency (ε) of providing an energy service (*s*) by $\zeta = \Delta \varepsilon / \varepsilon$ ($\zeta \ge 0$), thereby reducing the energy cost (p_s) of that service by $\tau = \Delta p_s / p_s$ ($\tau \le 0$). Let *Q* represent the household's baseline GHG emissions (direct plus embodied), ΔH the change in emissions that would occur *without* any behavioural responses to the lower cost energy service (the 'engineering effect'), ΔG the change in emissions that results from those behavioural responses (the 're-spending effect'), and $\Delta Q = \Delta H + \Delta G$ the net change in GHG emissions. The total rebound effect (R_T) is then given by:

$$R_T = \frac{\Delta H - \Delta Q}{\Delta H} = -\frac{\Delta G}{\Delta H}$$
 12

As discussed above, this is comprised of direct and indirect effects $(R_T = R_D + R_I)$ which may each be decomposed into income and substitution effects $(R_D = \hat{R}_D + \tilde{R}_D$ and $R_I = \hat{R}_I + \tilde{R}_I)$.

The baseline GHG emissions for the household may be written as:

$$Q = x_s u_s^x + \sum_{i(i \neq s)} u_i^x x_i$$
13

Where x_i is the expenditure on commodity *i* (in £), u_i^x is the GHG intensity of that expenditure (in tCO_{2e}/£) and x_s and u_s^x are the corresponding values of these variables for the energy service. The GHG intensities include both direct and embodied emissions

To estimate the engineering effect (ΔH), we assume the consumption of all commodities remains unchanged while the energy cost of the energy service falls. The change in expenditure on the energy service as a consequence of the engineering effect is then given by $\Delta x_s^H = q_s \Delta p_s$. Given that $\Delta p_s = \tau p_s$ and $\Delta H = u_s^x \Delta x_s^H$ we obtain the following expression for the engineering effect:

$$\Delta H = u_s^{\lambda} x_s \tau \tag{14}$$

To estimate the re-spending effect (ΔG), we must allow for the change in expenditure on each commodity group (Δx_i). The change in expenditure on the energy service itself as a consequence of the engineering effect is given by $\Delta x_s^G = p_s \Delta q_s$.¹¹ Adding in the change of expenditure on other commodity groups we obtain the following expression for the respending effect:

$$\Delta G = u_s^x \Delta x_s^G + \sum_{i(i \neq s)} u_i^x \Delta x_i$$
¹⁵

Assuming marginal changes, we can use elasticities to substitute for Δx_s^G and Δx_i in this equation:

¹¹ For the energy service itself, the total change in expenditure is the sum of the engineering and re-spending effects: $\Delta x_s = \Delta x_s^H + \Delta x_s^G$

$$\Delta G = u_s^x x_s \tau(\eta_{x_s, p_s} - 1) + \sum_{i(i \neq s)} u_i^x x_i \tau \eta_{x_i, p_s}$$
¹⁶

Substituting the expressions for ΔH (Equation 14) and ΔG (Equation 16) into Equation 12 and noting that $w_i = x_i / x$, we arrive at the following expression for the total rebound effect:

$$R_T = (1 - \eta_{x_s, p_s}) - \sum_{i(i \neq s)} \psi_i \eta_{x_i, p_s}$$
17

Where:

$$\psi_i = \frac{u_i^x w_i}{u_s^x w_s}$$
 18

Using Equations 9 to 11, the total rebound effect can also be expressed as:

$$R_T = -\eta_{q_s, p_s} - \sum_{i(i \neq s)} \psi_i \eta_{q_i, p_s}$$
¹⁹

The first term in Equation 19 is the direct rebound effect (R_D) and the second is the indirect effect (R_I) . The first depends solely upon the own-price elasticity of energy service demand (η_{q_s,p_s}) , while the second depends upon the elasticity of demand for commodity *i* with respect to the energy service (η_{q_i,p_s}) and the GHG intensity and expenditure share of that commodity relative to that of the energy service (ψ_i) . Hence, commodities with a small cross price elasticity may nevertheless contribute a large indirect rebound effect if they are relatively GHG intensive and/or have a large expenditure share (and vice versa).

Using the Slutsky equation, we decompose Equation 19 as follows:

$$R_{T} = \left[w_{s}\eta_{q_{s},x} - \tilde{\eta}_{q_{s},p_{s}}\right] + \left[\sum_{i(i\neq s)} \left[\psi_{i}w_{s}\eta_{q_{i},x} - \psi_{i}\tilde{\eta}_{q_{i},p_{s}}\right]\right]$$
20

As noted, the challenges of incorporating energy services within a household demand model make it difficult to implement this approach directly. Hence, in what follows we estimate the required elasticities with respect to energy commodities (l) rather than energy services (s). Table 5 summarises the required expressions.

Table 5 Analytical expressions for the components of the rebound effect

	Direct rebound effect	Indirect rebound effect for	
		commodity <i>i</i>	
Income effect	$\hat{R}_D = w_l \eta_{x_l, x}$	$\hat{R}_I = \psi_i w_l \eta_{x_i, x}$	
Substitution effect	$\widetilde{R}_D = 1 - \widetilde{\eta}_{x_l, p_l}$	$\widetilde{R}_I = -\psi_i \widetilde{\eta}_{x_i, p_l}$	

3.2 Econometric model

As with the other studies in Table 4, we base our household demand model on the *Linear Approximation to the Almost Ideal Demand System (LAIDS)*. This has become the model of choice in household demand analysis since it has number of advantages over competing approaches (Deaton and Muellbauer, 1980). As a compromise between resolution and degrees of freedom, we split household expenditure into 12 subcategories (Table 6) and assume separability to give a two-stage budgeting framework (Figure 1). Households are assumed to first allocate expenditure between four aggregate groups (r), and then distribute the group expenditures between individual commodities within each group (i). This framework allows expenditure on commodities within a group to be specified as a function of

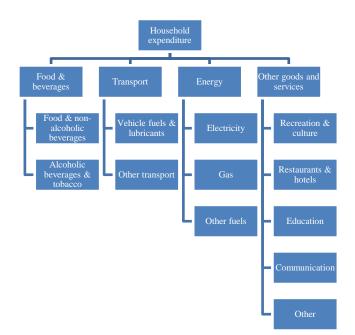
group expenditure and the prices of commodities within the group alone. As with Mizobuchi (2008), the commodity categories include both durables and nondurables.

Agg	gregate Group (r) Category (i)		COICOP	Description	
	Stage 1	Stage 2	category		
1.	Food and	1	1	Food and non-alcoholic beverages	
_	beverages	2	2	Alcoholic beverages, tobacco, narcotics	
2.	Transport	3	7.2.2.2	Vehicle fuels and lubricants	
		4	Rest of 7	Other transport	
3.	Energy	5	4.5.1	Electricity	
		6	4.5.2	Gas	
		7	4.5.3 and 4.5.4	Other fuels	
4.	Other goods and	8	9		
	services			Recreation & culture	
		9	11	Restaurants & hotels	
		10	10	Education	
		11	8	Communication	
		12		Other	
			3	Clothing and footwear	
			4.1 to 4.4	Other housing	
			5	Furnishings, household equipment &	
				household maintenance	
			6	Health	
			12	Miscellaneous goods and services	

Table 6 Categories of goods and services

Notes: COICOP - Classification of Individual Consumption According to Purpose. 'Other housing' includes rent, mortgage payments, maintenance, repair and water supply. 'Other transport' includes public transport, non-fuel expenditure on private vehicles and some aviation – although air travel for package holidays is included within 'recreation and culture'. 'Other fuels' include solids and liquids.

Figure 1 Two-stage budgeting model



Let x_t^r represent the expenditure on aggregate commodity group r in period t and w_t^r the fractional share of that group in total household expenditure (x_t):

$$w_t^r = \frac{x_t^r}{x_t}$$
 21

In the first stage of the AIDS model, this is specified as:

$$w_t^r = \alpha^r + \sum_{s=1,..4} \gamma^{rs} \ln p_t^s + \beta^r \ln(x_t / P_t) + \sum_{s=1,..3} \lambda^{rs} w_{t-1}^s + \varepsilon_t^r$$
22

Where: *r* and *s* index over the aggregate commodity groups; p_t^s is the price of the aggregate commodity group *s* in period *t*; x_t is total expenditure per household in that period; P_t is the Stone's price index for the aggregate commodities; w_{t-1}^s is the lagged expenditure share of commodity group *s*; α^r , γ^{rs} , β^r and λ^{rs} are the unknown parameters and ε_t^r is the error term. The Stone's price index is defined as:

$$\ln P_t = \sum_{r=1,.4} w_t^r \ln p_t^r$$
23

Given the constraints on degrees of freedom, we do not include additional covariates. However, our model departs from standard applications of LAIDS by including lagged expenditure shares (w_{t-1}^s) to capture the inertia in price responses - for example as a result of habit formation. The inclusion of lags also reduces problems of serial correlation (Edgerton, 1997; Klonaris and Hallam, 2003; Ray, 1983; Ryan and Plourde, 2009; Shukur, 2002). Since the lagged expenditure shares sum to unity, we only include three in each equation to avoid multi-collinearity.¹²

Restrictions are often imposed upon the parameter values to ensure the results are compatible with consumer demand theory. Specifically, *adding up* requires that expenditures on each commodity add up to total expenditure; *homogeneity* requires that quantity demanded remains unchanged if prices and total expenditure change by an equal proportion; and *symmetry* requires that the compensated cross-price elasticities between two commodities are equal. These may be implemented as follows:

Adding up:
$$\sum_{r} \alpha^{r} = 1; \sum_{r} \beta^{r} = 0; \sum_{r} \gamma^{rs} = 0 \quad s = 1,..4; \text{ and } \sum_{r} \lambda^{rs} = 0 \quad s = 1,..3;$$

Homogeneity: $\sum_{r} \gamma^{rs} = 0 \ s = 1,..4;$ Symmetry: $\gamma^{rs} = \gamma^{sr}$

¹² An alternative to dropping the lagged budget share of one commodity would be to impose the restriction: $\sum_{s} \lambda^{rs} = 0$. This would not affect the estimated coefficients.

The second stage of the AIDS model distributes the group expenditures (x_t^r) between individual commodities within each group. Let x_{it}^r represent expenditure on commodity *i* in aggregate group *r* during period *t* ($i \in r$) and w_{it}^r represent the fractional share of that commodity in the expenditure on group $r(x_t^r)$:

$$w_{it}^r = \frac{x_{it}^r}{x_t^r}$$

This is specified as:

$$w_{it}^{r} = \alpha_{i}^{r} + \sum_{j=1,..,k^{r}} \gamma_{ij}^{r} \ln p_{ij}^{r} + \beta_{i}^{r} \ln(x_{t}^{r} / P_{t}^{r}) + \sum_{j=1,..,k^{r-1}} \lambda_{ij}^{r} w_{jt-1}^{r} + \varepsilon_{it}^{r}$$
25

Where: *i* and *j* index over the commodities within aggregate group r (*i*, $j \in r$); k^r is the number of commodities in aggregate group r; p_{it}^r is the price of commodity *i* in period *t*; x_t^r is expenditure on group r in that period; P_t^r is the Stone's price index for group r; α_i^r , γ_{ij}^r β_i^r and λ_{ij}^r are the unknown parameters and ε_{it}^r is the error term. The Stone's price index for group r index for group r is defined as:

$$\ln P_t^r = \sum_{i=1,..k^r} w_{it}^r \ln p_{it}^r$$
26

Again, the adding up, symmetry and homogeneity restrictions can be imposed as follows:

Adding up:
$$\sum_{i} \alpha_{i}^{r} = 1; \sum_{i} \beta_{i}^{r} = 0; \sum_{i} \gamma^{ij} = 0; j = 1, ...k^{r} \text{ and } \sum_{i} \lambda_{ij}^{r} = 0 \quad j = 1, ...k^{r} - 1$$

Homogeneity:
$$\sum_{i} \gamma_{ij}^{r} = 0$$
 $j = 1,..k^{r}$ Symmetry: $\gamma_{ij}^{r} = \gamma_{ji}^{r}$

Alternatively, an unrestricted model can be estimated for both first and second stage and the homogeneity and symmetry restrictions tested. It is common for these restrictions to be rejected in empirical studies (Keuzenkamp and Barten, 1995).¹³ The adding up restriction, however, is always satisfied by dropping one of the equations.

Godard (1983) derives equations for estimating the short run expenditure and price elasticities for a single stage LAIDS model¹⁴, while Edgerton (1997) derives expressions for a two-stage model. In the latter, 'total' elasticities are calculated from estimates of the 'between-group' and 'within-group' elasticities. The interpretation of these is summarised in Box 1 while the relevant formulae are summarised in Table 7 (Edgerton, 1997). Here, δ_{rs} (Kronecker delta) is equal to unity when r=s (i.e. own-price elasticity) and zero otherwise. Similarly, δ_{ij}^{r} is unity when i=j and zero otherwise.

¹³For example, the foundational *AIDS* study by Deaton and Muellbauer (1980) rejected these restrictions.

¹⁴ Buse (1994) evaluates several elasticity expressions for LAIDS model and finds these expressions are marginally the best.

Box 1 Interpretation of the between-group, within-group and total elasticities

- 1. *Between-group* expenditure $(\eta_{x_r,x})$ and price $(\eta_{x_r,p_s} \text{ and } \tilde{\eta}_{x_r,p_s})$ elasticities for the aggregate commodity groups (r) respectively indicate how expenditure on aggregate group *r* changes following: a) a change in total expenditure; and b) a change in the price of aggregate group *s* holding total expenditure fixed.
- 2. *Within-group* expenditure (η_{x_i,x_r}^r) and price (η_{x_i,p_j}^r) and $\tilde{\eta}_{x_i,p_j}^r)$ elasticities for each commodity *i* within aggregate group *r* respectively indicate how expenditure on this commodity changes following: a) a change in expenditure on group *r*; and b) a change in the price of commodity *j* within aggregate group *r* holding expenditure on group *r* fixed. Here, both *i* and *j* are within the same aggregate group.
- 3. *Total* expenditure $(\eta_{x_i,x})$ and price (η_{x_i,p_j}) and $\tilde{\eta}_{x_i,p_j}$ elasticities for each commodity *i* within aggregate group *r* respectively indicate how expenditure on this commodity changes following: a) a change in total expenditure; and b) a change in the price of commodity *j* holding total expenditure fixed but allowing expenditure on group *r* to vary. Here, *i* and *j* may be within the same or different aggregate group.

Elasticity	Between-group	Within-group $(i, j \in r)$	Total
Expenditure	$\eta_{x_r,x} = 1 + \frac{\beta^r}{w^r}$	$\eta_{x_i,x_r}^r = 1 + \frac{\beta_i^r}{w_i^r}$	$\eta_{x_i,x} = \eta_{x_i,x_r}^r \eta_{x_r,x}$
Uncompensated price	$\eta_{x_r, p_s} = \frac{\gamma^{rs} - \beta^r w_s}{w_r} - \delta_{rs}$	$\eta_{x_i,p_j}^r = \frac{\gamma_{ij}^r - \beta_i^r w_j^r}{w_i^r} - \delta_{ij}^r$	$\eta_{x_i,p_j} = \delta_{rs}\eta_{x_i,p_j}^r + \eta_{x_i,x_r}^r(\delta_{rs} + \eta_{x_r,p_s})w_j^s$
Compensated price	$\widetilde{\eta}_{x_r,p_s} = \frac{\gamma^{rs}}{w_r} + w_s - \delta_{rs}$	$\widetilde{\eta}_{x_i,p_j}^r = \frac{\gamma_{ij}^r}{w_i^r} + w_j^r - \delta_{ij}^r$	$\widetilde{\eta}_{x_i,p_j} = \delta_{rs} \widetilde{\eta}_{x_i,p_j}^r + \eta_{x_i,x_r}^r (\delta_{rs} + \widetilde{\eta}_{x_r,p_s}) w_j^s$

Table 7: Analytical expressions for the between-group, within-group and total elasticities within a two-stage LAIDS model

Source: Edgerton (1997); Goddard (1983)

The formulae in Table 7 deserve some explanation. The formula for the total expenditure elasticity for the *i*th commodity in the *r*th group (Table 7, line 2) is simply the product of the within-group elasticity for that commodity and the expenditure elasticity of the group.

The formula for the total uncompensated price elasticity (Table 7, line 3) is more complex. Note first that when commodities *i* and *j* are in different groups, $\delta_{rs} = 0$ and the expression reduces to:

$$\eta_{x_i, p_j} = \eta_{x_i, x_r}^r \eta_{x_r, p_s} w_j^s$$
²⁷

Here, the first term (η_{x_i,x_r}^r) represents the change in expenditure on commodity *i* following a change in expenditure on group *r*; the second term represents the change in expenditure on group *r* following a change in the price of group *s*; and the third term represents the share of commodity *j* in the expenditure on group *s*. As shown by Edgerton (1997), the latter is equivalent to the change in the price of group *s* following a change in the price of commodity *j* ($w_j^s = \partial \ln p_s / \partial \ln p_j$).

When *i* and *j* are in the same group (r=s), the expression becomes:

$$\eta_{x_i, p_j} = \eta_{x_i, p_j}^r + \eta_{x_i, x_r}^r (1 + \eta_{x_r, p_r}) w_j^r$$
28

Here, the total cross price elasticity equals the within-group cross price elasticity (η_{x_i,p_j}^r) , plus a product of three factors. The first of these (η_{x_i,x_r}^r) measures the change in expenditure on commodity *i* following a change in expenditure on group *r*; the second measures the change in expenditure on group *r* following a change in the price of group *r*; and the third represents the change in the price of group *r* following a change in the price of commodity *j* $(w_j^r = \partial \ln p_r / \partial \ln p_j)$. The smaller each of these terms are, the smaller the difference between the within-group and total price elasticity. The formula for the total compensated price elasticity (Table 7, line 4) follows a similar pattern.

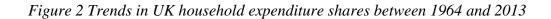
Following standard practice, we estimate the elasticities using the mean values of the expenditure shares over the full time series. The total elasticities are used for estimating rebound effects.

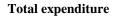
3.3 Data

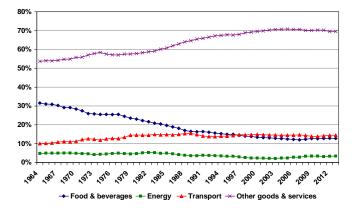
Data for the price of different commodity groups and household expenditure on those groups is taken from *Consumer Trends*, published by the UK Office of National Statistics (ONS). The period chosen is 1964 to 2013 and the values are converted to current prices using a base year of 2010. Data on total household numbers for selected years is taken from DGLC (2014), with data on intermediate years estimated by linear interpolation.¹⁵ Figure 2 indicates the change in expenditure shares over this period both between and within-groups. During this period, the share of food in total expenditure almost halved, the share of transport increased by 50% and the share of energy fell by 30%. Within the energy group, substitution by gas reduced the expenditure share of other fuels (coal and oil) from 42% in 1964 to 6% in 2013.¹⁶

¹⁵ Two sets of time series data for expenditure and implied deflators are available: a) 1964 to 2010 consistent with the UK National Accounts for 2010 (ONS, 2010) and b) 1997 to 2013 consistent with the National Accounts for 2011 (ONS, 2011). To create a consistent time series over the full period, we take the annual growth rates of expenditure and deflators during 1964-1997 from ONS (2010) and use these to adjust the 1997 data from ONS (2011).

¹⁶ Since our analysis uses mean values of expenditure shares, the estimated contribution of other fuels is larger, and the estimated contribution of transport is lower, than would be the case if we had used 2013 values of expenditure shares.

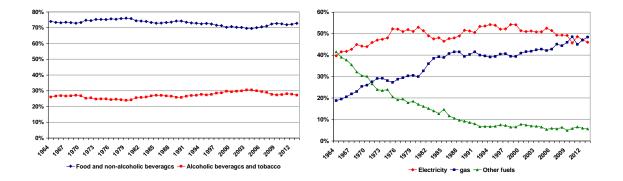






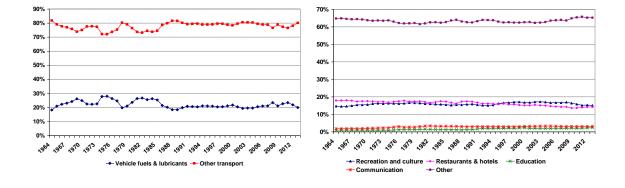
Food and non-alcoholic beverages







Other goods and services



Our data source for the GHG emissions associated with different categories of goods and services is the *Surrey Environmental Lifestyle Mapping Framework* (SELMA). This is a quasi-multi-regional, environmentally extended input-output model that provides estimates of the GHG intensity of UK household expenditure in each category (in tCO₂e/£) for 2004 (Druckman and Jackson, 2008).¹⁷ These figures include both the *direct* emissions from the consumption of electricity¹⁸, heating fuels and vehicle fuels, and the *embodied* emissions from each stage of the supply chain for goods and services – which may occur either in the UK or overseas. We adjust these estimates to allow for the emissions associated with government expenditure of product taxation revenues.¹⁹

Figure 3 (top) shows that expenditure on electricity, gas and other fuels is approximately twice as GHG intensive as expenditure on vehicle fuels and approximately four times as GHGs intensive as expenditure on other transport – which is the next most GHG intensive category. Overall, expenditure on energy commodities is approximately five times as GHG intensive as the share-weighted mean. But the high GHG intensity of energy commodities is offset by their small share of total expenditure (7% - Figure 3, middle), with the result that direct energy consumption only accounts for 27% of an average household's 'GHG footprint'

¹⁷ The GHG intensity of a category is estimated from the GHG emissions associated with that category in 2004 (obtained from SELMA) divided by 'real' expenditure on that category in 2004 (reference year 2013). The exception is electricity where emissions are estimated from 2012 electricity consumption (in kWh) multiplied by an emission factor for 2012 (kgCO₂e/kWh). This adjustment is designed to reflect the large reduction in the GHG intensity of electricity

¹⁸ Emissions from electricity consumption are commonly labelled as direct, although they occur at the power station.

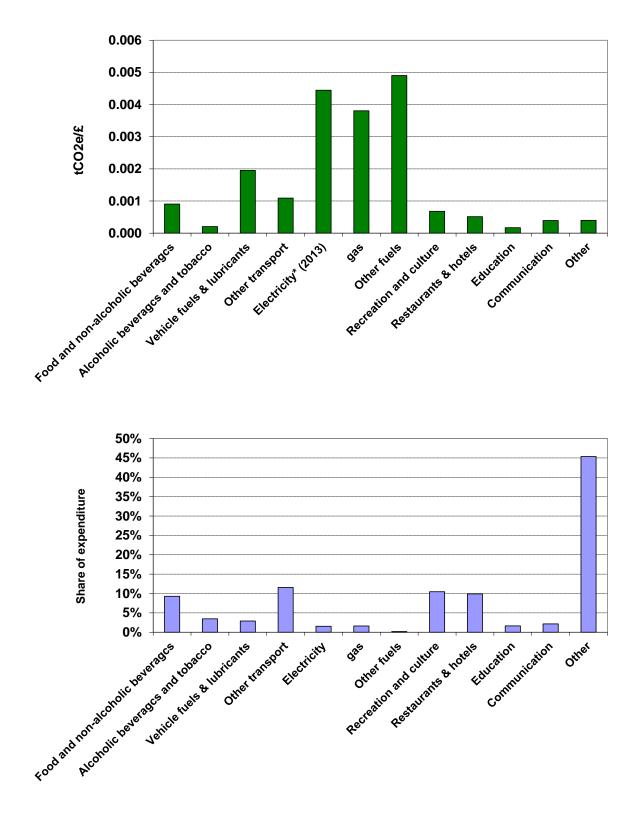
¹⁹ Environmentally-Extended Input-Output (IO) models such as SELMA only include the GHG emissions associated with each expenditure category. But expenditures on different commodities include various taxes (such as Value Added Tax - VAT) which in turn are used to fund government expenditure. Since government spending is a separate category in the national accounts, the associated GHG emissions are normally excluded from the estimated GHG intensities of household expenditure. Exclusion of these emissions could bias estimates of rebound effects, in particular because differing levels of product taxation are applied to different goods and services. For example, in the UK there is 20% VAT on most goods and services; 5% VAT on electricity, gas and other fuels; zero rate VAT on most food products; and around 65% taxation on vehicle fuels. To eliminate this potential bias we: first, estimate the GHG intensity of UK government expenditure in 2004; second, use this to estimate the GHG emissions associated with taxation in each category; and third, add these to the emissions provided by SELMA for each expenditure category. This in turn leads to an adjusted GHG intensity of expenditure for each category which is used in the calculation of rebound effects. As the GHG intensity of government expenditure is relatively low, this adjustment does not significantly change our results.

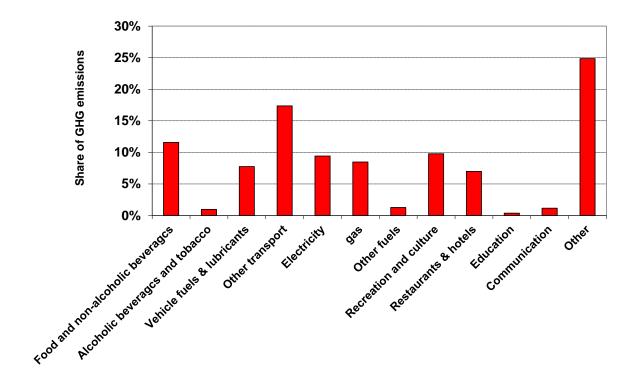
(Figure 3, bottom), split between 19% domestic energy (i.e. electricity, gas and other fuels) and 8% vehicle fuels.

The category providing the largest single contribution (25%) to total emissions is 'other goods and services' which includes expenditure on clothing, housing maintenance, water and furnishings and accounts for 45% of expenditure. The next highest is 'other transport' (12%) which includes non-fuel costs for private cars, public transport and some air travel. Since these categories have both a relatively high expenditure share and a relatively high GHG intensity they provide a significant contribution to total emissions (42%).

Our estimates of GHG intensities allow for the variation of product taxation between categories: namely VAT exemption for food and non-alcoholic beverages, lower rate VAT for domestic energy and high taxation of vehicle fuels (~60% of retail price). The latter contributes to the comparatively low GHG intensity of vehicle fuels compared to domestic energy.

Figure 3 GHG intensity of expenditure, share of total expenditure and share of total GHG emissions by category for an average household





4 Results

4.1 Econometric results

The two-stage budgeting assumptions model in Figure 1 leads to a total of 16 equations in five groups. The equations in each group are estimated as a system using the Iterative Seemingly Unrelated Regressions (ISUR) method which is suitable for imposing cross-equation restrictions and corrects the estimates for any correlation of the error terms between equations. The adding up restriction is imposed by dropping one of the equations in each group.

The equations in each group are first estimated without imposing homogeneity and symmetry restrictions. A Wald test is then used to test for these restrictions both individually and in combination. If homogeneity and/or symmetry are not rejected then they are imposed on the relevant group.

Annex 1 summarises the parameter estimates for each group of equations and the results of the restrictions. Annex 2 summarises the between-group elasticity estimates, and Annex 3 summarises the within-group estimates. The most relevant results are the total elasticity estimates for the energy and transport groups which are summarised in Tables 8 to 10. For ease of interpretation, all elasticities are expressed for quantities (q) rather than expenditure shares (w).

Looking first at Annex 1 (Tables A.1 to A.5), we see that the overall fit of the equations is good, with more than two thirds of the parameter estimates being statistically significant at the 5% level and with most of the equations having an adjusted R^2 exceeding 90%. From Table A.6 we see that both homogeneity and symmetry restrictions are rejected for the energy group, hence we use the non-restricted results for this group. For all other groups only the homogeneity restriction cannot be rejected. Hence, we impose homogeneity in all non-energy groups, but we do not impose symmetry on any group. We also use the Portmanteau serial correlation test for each group and find no evidence of serial correlation.

Looking at the total elasticity estimates (Tables 8-10), we make several observations. First, the expenditure elasticities for domestic energy are relatively low -0.07 for electricity and 0.15 for gas. These values are broadly comparable with those estimated from cross-sectional data in our previous work (Chitnis et al., 2014) where we showed that high-income groups have very low expenditure elasticities for these commodities – which in turn has a disproportionate influence on the overall mean. In contrast, the estimated expenditure elasticities for vehicle fuels, 'other transport' and the sub-categories of 'other goods and services' all exceed unity, indicating that they are luxury goods.

Second, the own-price elasticities for energy commodities have the expected sign with values of -0.39 for electricity, -0.59 for gas and -0.59 for vehicle fuels. For comparison, a review of studies by Espey and Espey (2004) found a mean short-run elasticity of -0.35 (median -0.28) for electricity; a study by Asche et al. (2008)found short run elasticities of household natural gas demand to be -0.25 or less; and a review of studies by Goodwin et al. (2004) found a mean short-run elasticity for vehicle fuels of -0.25. Hence, our estimates appear to be at the high end of the range found in the literature - especially for gas and vehicle fuels. Since the expenditure elasticities for these commodities are relatively small, the own-price response is primarily driven by substitution effects – as is indicated by the near equivalence of the compensated and uncompensated elasticities for these commodities (Tables 9 and 10).

Third, electricity and gas are found to be substitutes, and both of these are estimated to be substitutes for vehicle fuels when the price of the latter changes, but complements when their own-price changes (symmetry is not imposed). In addition, both 'other transport' and all subcategories within 'other goods and services' are estimated to be complements to energy commodities and will therefore contribute a negative indirect rebound effect. In contrast, food and drink products are estimated to be substitutes and will contribute a (small) positive indirect rebound effect.

Overall, the results suggest that the substitution effects for energy commodities outweigh the income effects, and changes in the price of one or more energy commodities will have their largest impact on the quantity of energy commodities demanded. Since energy commodities are also GHG intensive, they are likely to dominate the total rebound effect. This is demonstrated below, where we report the rebound results.

Table 8 Total expenditure elasticities (η_{q_ix})

	Er	nergy		Transport		Food and beverages		Other goods and services				
	Electricity	Gas	Other fuels	Vehicle fuels	Other transport	Food & non- alcoholic beverages	Alcoholic beverages & tobacco	Recreation and culture	Restaurants and hotels	Education	Communication	Other
Expenditure elasticity	0.07	0.15	0.16	1.01	1.33	0.71	0.88	1.22	1.15	1.23	1.06	1.01

Table 9 Total compensated cross price elasticities- energy group ($\tilde{\eta}_{\mathbf{q}_i\mathbf{p}_j})$

	E	nergy		Tran	isport	Food and	l beverages	Other goods and services					
	Electricity	Gas	Other	Vehicle	Other	Food and	Alcoholic	Recreation	Restaurants	Education	Communication	Other	
			fuels	fuels	transport	non-	beverages &	and culture	and hotels				
						alcoholic	tobacco						
						beverages							
Electricity	-0.39	0.11	-0.08	-0.04	-0.06	0.04	0.05	0.01	0.01	0.01	0.01	0.01	
Gas	0.07	-0.58	0.37	-0.03	-0.04	0.03	0.03	0.01	0.01	0.01	0.01	0.01	
Other	0.04	0.12	-0.76	-0.01	-0.02	0.01	0.01	0.003	0.003	0.003	0.003	0.003	
fuels													
Vehicle	0.07	0.15	0.16	-0.55	0.04	0.01	0.01	0.01	0.01	0.01	0.01	0.01	
fuels													

	E	nergy		Trar	nsport	Food and I	beverages		Other good	s and service	s	
	Electricity	Gas	Other	Vehicle	Other	Food and non-	Alcoholic	Recreation	Restaurants	Education	Comms	Other
			fuels	fuels	transport	alcoholic	beverages &	and culture	and hotels			
						beverages	tobacco					
Electricity	-0.39	0.10	-0.08	-0.06	-0.08	0.02	0.03	-0.01	-0.01	-0.01	-0.01	-0.01
Gas	0.07	- 0.59	0.36	-0.05	-0.06	0.02	0.02	-0.01	-0.01	-0.01	-0.01	-0.01
Other												-
fuels	0.04	0.12	-0.76	-0.02	-0.02	0.01	0.01	-0.004	-0.003	-0.003	-0.003	0.004
Vehicle fuels	0.07	0.15	0.16	-0.59	-0.001	-0.01	-0.01	-0.03	-0.02	-0.02	-0.02	-0.03

Table 10 Total uncompensated cross price elasticities-energy group ($\eta_{q_i p_j}$)

4.2 Estimates of rebound effects

The estimated rebound effects are presented in four ways to illustrate both their magnitude and their underlying drivers. Specifically, we indicate the relative contribution of: a) income and substitution effects; b) direct and indirect rebound effects; c) direct and embodied emissions; and d) individual commodities.

Our estimates of the *total* rebound effect are 63% for gas, 53% for electricity and 46% for vehicle fuels, (Figure 4). These estimates are larger than many in the literature, although smaller than those by Brannlund *et al* (2007) and Mizobuchi (2008). Net substitution across all commodities accounts for between two thirds and three quarters of the total rebound for electricity and gas, but only one fifth for vehicle fuels. This demonstrates the importance of capturing substitution effects and suggests that studies that only estimate income effects could underestimate the total rebound - particularly for electricity and gas.

Our estimates of *direct* rebound effects are 59% for vehicle fuels, 58% for gas and 41% for electricity (Figure 5) - indicating that they account for the majority of the total rebound. For vehicle fuels, the direct rebound effect *exceeds* the total rebound effect, since the indirect rebound effect is negative. These estimates are at the high end of the range in the literature, particularly for vehicle fuels where most (primarily US) studies estimate direct rebound effects of 20% or less (Sorrell and Dimitropoulos, 2007b). Figure 6 demonstrates that the income effects mostly derive from other commodities (indirect rebound) while the substitution effects mostly derive from the energy service itself (direct rebound). Again, studies that only estimate income effects could erroneously conclude that the indirect rebound effect accounts for the majority of the total rebound - whereas these results show the opposite.

Direct emissions from energy commodities account for between two thirds and three quarters of the total rebound (Figure 7). This follows directly from the above, since it is the direct rebound effect that dominates the overall rebound effect and this is wholly direct emissions. Reduced consumption of other energy commodities slightly reduces the total rebound effect for electricity and gas but has a greater impact on the total rebound for vehicle fuels. Income effects are dominated by embodied emissions (i.e. non-energy commodities) while substitution effects are dominated by direct emissions (i.e. energy commodities) (Figure 8). Since the latter is larger than the former, substitution both within and between energy commodities have the dominant influence on the overall results. Again, studies that neglect substitution effects could erroneously conclude that the total rebound effect consists primarily of embodied emissions - whereas these results show the opposite.

Finally, Figure 9 illustrates the relative contribution of different commodities to the total rebound (normalised to 100%). This again shows the dominance of own-price effects. Substitution between electricity and gas dampens the rebound effect for these two commodities, as does substitution away from food and beverages. In contrast, the complementary relationship between energy commodities and both 'other transport' and 'other goods and services' contributes a positive rebound effect. For vehicle fuels, substitution away from electricity and gas significantly reduces the total rebound.

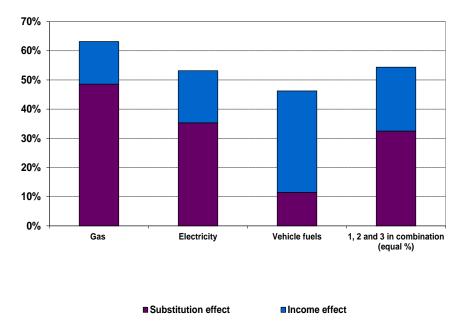
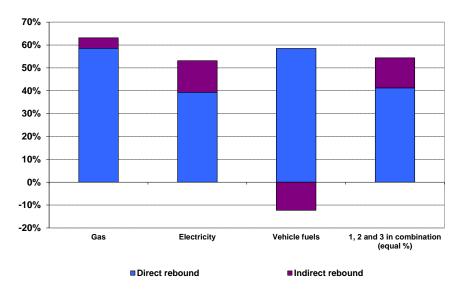


Figure 4 Estimated rebound effects – split by net income and substitution effects

Figure 5 Estimated rebound effects - split by direct and indirect rebound effects





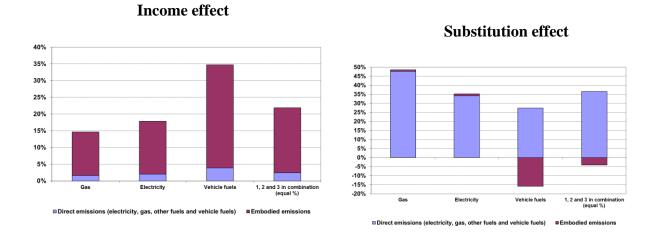
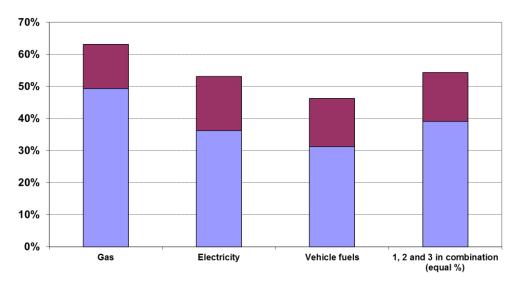


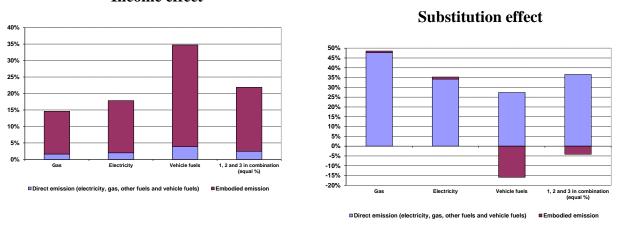
Figure 7 Estimated rebound effects - split by direct and embodied emissions



■ Direct emissions (electricity, gas, other fuels and vehicle fuels) ■ Embodied emissions

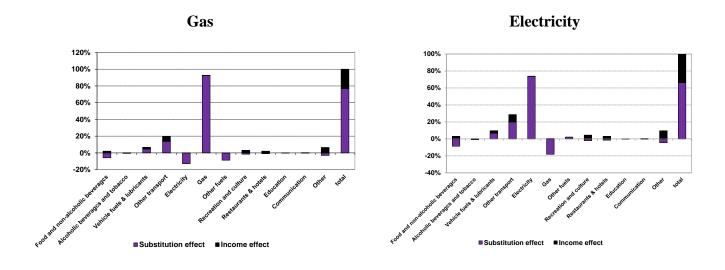
Figure 8 Net income and substitution rebound effects - split by direct and embodied

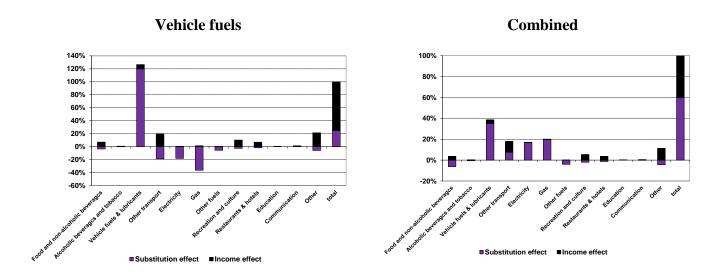
emissions



Income effect

Figure 9 Contribution of different commodity groups to the total rebound effect





5 Discussion

In our previous study of combined direct and indirect rebound effects for UK households (Chitnis et al., 2014) we concluded that the total rebound effect was modest (0-32%) for measures affecting domestic energy use and larger (25-65%) for measures affecting vehicle fuels, and that it primarily derived from increased consumption of non-energy goods and services. We further suggested we may have *underestimated* the total rebound since we did not model substitution effects.

The present study shows that this suggestion was correct. By using price rather than expenditure elasticities, we now estimate significantly larger rebound effects, namely 63% for domestic gas use, 53% for electricity and 46% for vehicle fuels. The primary source of this rebound is increased consumption of cheaper energy services (i.e. direct rebound), and this is primarily driven by substitution effects. A clear implication of this finding is that studies that ignore substitution effects (e.g. those in Table 3) will underestimate the total rebound.

In practice, many studies focus solely upon direct rebound effects and estimate these from time-series data on individual energy services (e.g. transport, heating). Since, by definition, these neglect indirect rebound effects, their results may also underestimate the total rebound (unless, that is, the indirect rebound effect is negative). However, our results suggest that such studies may provide a better approximation to the total rebound effect than do studies that estimate the latter using only expenditure elasticities. Since the direct rebound effect appears larger than the indirect rebound effect, errors in estimating the former will matter more than errors in estimating the latter.

We suspect, however, that the present study (along with others in Table 4) may *overestimate* the total rebound effect. The primary reason for this is that we assume the own-price elasticity of energy demand to be equivalent to the efficiency elasticity of energy service demand ($\eta_{q_e,\mathcal{E}} = \eta_{q_e,p_e}$) and therefore to provide a suitable measure of the direct rebound effect. As Sorrell and Dimitropoulos (2007a) show, this equivalence only holds if energy prices are exogenous, energy service demand depends only on energy service prices (p_s) and energy efficiency is constant. Absent these conditions, the own-price elasticity of energy demand will overestimate the direct rebound effect (Sorrell and Dimitropoulos, 2007a). Factors such as the endogeneity of energy efficiency and the asymmetric response of consumers to changes in energy prices may exacerbate this bias (Sorrell and Dimitropoulos, 2007a). Hence, the simplicity of using energy commodities rather than energy services in the demand model comes at a cost.

A further bias may arise when energy commodities provide *multiple* energy services (Chan and Gillingham, 2014). For example, if electric heating is a complement (substitute) to lighting, the own-price elasticity of electricity may overestimate (underestimate) the direct rebound effect for each. Hunt and Ryan (2014) explore this point by estimating a LAIDS model of household energy purchases that includes covariates that they assume to be correlated with energy efficiency.²⁰ Although not equivalent to including energy services within the demand model, their approach leads to *lower* estimates of energy price elasticities than specifications in which these covariates are omitted. This further suggests that the specification used here may overestimate energy price elasticities and hence also the total rebound effect.

We further observe that our estimates of energy price elasticities are at the high end of the range found in the literature. Lower estimates of these elasticities would lead to lower estimates of the direct rebound effect – and correspondingly higher estimates of the indirect rebound effect. Since energy commodities are relatively GHG intensive, the former is likely to outweigh the latter leading to a lower estimate of the total rebound.

Further caveats relate to the methodological trade-offs discussed in section 2.3 - including the limited number of commodity groups employed, the potential sensitivity of the results to separability assumptions and the absence of socio-economic covariates. Our methodology also neglects any supply-side responses to improved energy efficiency which may modify the estimated effects. The likely direction of bias from these sources is ambiguous, although they all represent important avenues for future research. But the priority is to find ways of incorporating energy services directly within a household demand model.

6 Summary

This study adds to a small but growing volume of evidence that estimates combined direct and indirect rebound effects for households. We extend the existing literature by estimating a

²⁰. Hunt and Ryan try three approaches, namely: a simple time trend; historic energy prices; and historic energy prices allowing for asymmetric responses.

full household demand model and identifying the relative contribution of different mechanisms to the results. Our results suggest a total rebound effect of 63% for measures affecting domestic gas use, 53% for measures affecting electricity use and 46% for measures affecting vehicle fuel use. The primary source of this rebound is increased consumption of cheaper energy services (i.e. direct rebound) and this in turn is primarily driven by substitution effects. Our results suggest that previous studies that neglected substitution effects may have underestimated the total rebound effect. However, we have identified a number of reasons why our estimates may be upwardly biased. To reduce this risk, future research should give priority to including energy services directly within a household demand model.

Acknowledgments

This research was supported by funding from the UK Department of Environment Food and Rural Affairs (DEFRA), the UK Economic and Social Research Council (ESRC) and the Scottish Government as part of the <u>Sustainable Lifestyles Research Group</u> (SLRG). Completion of the research was funded by the Research Councils UK through their support for the <u>Centre on Innovation Energy Demand</u> (Grant No. EP/KO11790/1). Earlier versions of this paper were presented at IAEE conferences in Düsseldorf (August 2013), New York (June 2014) and Rome (October 2014) and at a BIEE conference in Oxford (September 2014). The authors would like to thank Lester Hunt and Euan Phimister for invaluable discussions. The usual disclaimers apply.

Annex 1 – Parameter estimates and restrictions tests

	α^r	β^r		7	rs, rs			λ^{rs}		\overline{R}^{2}
			Energy	Transport	Food and beverages	Other goods and services ²	Energy	Transport	Food and beverages	
Energy	-0.02 (-5.1)**	-0.03 (-6.6)**	0.02 (10.0)**	0.01 (3.0)**	-0.03 (-4.0)**	-0.01	0.13 (1.6)*	0.06 (2.1)**	0.05 (3.0)**	0.99
Transport	0.06 (4.9)**	0.04 (2.8)**	-0.02 (-3.5)**	0.06 (5.2)**	-0.03 (-1.9)**	-0.01	0.83 (4.4)**	0.70 (10.6)**	-0.004 (-0.1)	0.96
Food and beverages	0.01 (0.5)	-0.05 (-3.4)**	0.01 (1.4)	-0.02 (-1.4)	0.06 (3.6)**	-0.05	-0.77 (-4.2)**	-0.07 (-1.1)	0.83 (19.3)**	0.99
Other goods and services ¹	0.96	0.05	-0.01	-0.06	0.001	0.07	-0.19	-0.69	-0.88	_

Table A.1 Parameter estimates from first stage equations

Notes:

- \overline{R}^2 is the adjusted coefficient of determination.
- *t*-values in parenthesis. ** and * indicate statistical significance at 5% and 10% probability levels respectively.
- Coefficients for 'other goods & services' are estimated from the adding-up and homogeneity restrictions.
- The lagged budget share of 'other goods & services' is dropped to avoid co-linearity.

	$lpha_i^r$	eta_i^r		γ_{ij}^r		λ_{i}^{i}	r İj	\overline{R}^2
			Electricity	Gas	Other fuels ¹	Electricity	Gas	
Electricity	-0.65	-0.19	0.11	-0.11	-0.04	0.56	0.34	0.91
	(-3.6)**	(-4.6)**	(6.1)**	(-6.0)**	(-2.8)**	(6.8)**	(5.0)**	
Gas	0.50	0.13	-0.06	0.08	0.01	0.20	0.62	0.98
	(2.8)**	(3.0)**	(-3.3)**	(4.4)**	(1.0)	(2.3)**	(8.8)**	
Other fuels ¹	1.15	0.06	-0.05	0.03	0.02	-0.76	-0.96	

Table A.2 Parameter estimates from second stage equations – energy group

Notes:

• Coefficients for 'other goods & services' are estimated from the adding-up restriction.

• The lagged budget share of 'other goods & services' is dropped to avoid co-linearity.

Table A.3 Parameter estimates from second stage equations – transport group

	$lpha_i^r$	β_i^r		γ_{ij}^r	λ_{ij}^r	\overline{R}^{2}
			Vehicle	Other	Vehicle	
			fuels	transport ²	fuels	
Vehicle	-0.003	-0.04	0.07	-0.07	0.46	0.74
fuels	(-0.2)	(-5.5)**	(5.1)**	(-5.1)**	(5.4)**	
Other	1.00	0.04	-0.07	0.07	-0.46	_
transport ¹						

Notes:

• Coefficients for 'other transport' are estimated from the adding-up and homogeneity restrictions.

• The lagged budget share of 'other transport' is dropped to avoid co-linearity.

Table A.4 Parameter estimates	from second	l stage equations –	- food and beverages group
	J		Jeen meeter and a grant

	α_i^r	β_i^r	2	′ ^r ij	λ_{ij}^r	\overline{R}^2
			Food and	Alcoholic	Food and	
			non-	beverages	non-	
			alcoholic	and	alcoholic	
			beverages	tobacco ²	beverages	
Food and	0.16	-0.05	0.03	-0.03	0.58	0.91
non-alcoholic	(2.6)**	(-1.5)	(2.6)**	(-2.6)**	(3.9)**	
beverages						
Alcoholic	0.84	0.05	-0.03	0.03	-0.58	_
beverages						
and tobacco ¹						

Notes:

• Coefficients for 'alcoholic beverages and tobacco' are estimated from the adding-up and homogeneity restrictions.

• The lagged budget share of 'alcoholic beverages and tobacco' is dropped to avoid co-linearity.

	α_i^r	β_i^r			γ_{ij}^r					λ^r_{ij}		\overline{R}^2
			Recreation	Restaurants	Education	Communication	Other	Recreation	Restaurants	Education	Communication	
			& culture	& hotels				& culture	& hotels			
Recreation &	0.06	0.02	0.07	-0.03	0.03	-0.03	-0.32	0.67	0.07	-0.01	0.46	0.90
culture	(2.7)**	(3.1)**	(5.6)**	(-3.3)**	(4.2)**	(-5.0)**		(10.0)**	(0.7)	(-0.1)	(2.6)**	
Restaurants &	0.11	0.01	0.03	-0.001	0.01	0.001	-0.26	-0.1	0.40	-0.30	0.22	0.94
hotels	(3.8)**	(1.2)	(1.7)*	(-0.1)	(0.6)	(0.1)		(-1.0)	(2.3)**	(-1.3)	(0.9)	
Education	-0.01	0.002	-0.01	-0.002	0.004	0.01	-0.27	0.02	0.12	1.05	-0.26	0.98
	(-1.7)*	(1.1)	(-1.6)*	(-0.6)	(1.9)**	(3.0)**		(1.3)	(4.6)**	(22.0)**	(-5.0)**	
Communication	-0.02	-	-0.02	0.01	-0.01	0.02	-0.05	0.18	-0.01	0.27	0.45	0.97
	(-	0.0003	(-4.8)**	(3.3)**	(-2.5)**	(7.4)**		(7.2)**	(-0.4)	(4.4)**	(6.8)**	
	2.1)**	(-0.1)										
Other	0.85	-0.04	-0.10	0.04	-0.05	0.02	-0.84	-0.80	-0.58	-1.00	-0.87	

Table A.5 Parameter estimates from second stage equations – other goods and services group

Notes:

• Coefficients for 'other' are estimated from the adding-up and homogeneity restrictions.

• The lagged budget share of 'other' is dropped to avoid co-linearity.

Restriction	Aggregate	Food and	Transport	Energy	Other goods
	groups	beverages			and services
Symmetry	33.5*			5.4*	41.4^{*}
Homogeneity	5.7	1.2	2.7	27.8*	4.7
Symmetry and	45.4*			27.8^{*}	58.3 [*]
homogeneity					
combined					
Symmetry	39.0*				53.2*
with					
homogeneity					
imposed					
Notes					

Table A.6 Results of Wald test for symmetry and homogeneity restrictions

Notes:

• The restriction is the null hypothesis. * indicates that rejection of the null hypothesis significant at the 5% level.

• Symmetry tests not feasible for food and beverages and transport since there are only two equations in each group and one is dropped to satisfy adding up.

Annex 2 – Between-group elasticity estimates

Table A.7 Between-group expenditure elasticities ($\eta_{q_r x}$)

	Expenditure elasticity
Energy	0.11
Transport	1.26
Food and beverages	0.75
Other goods and services	1.07

Table A.8 Between-group compensated price elasticities ($\tilde{\eta}_{q_r p_s}$)

	Energy	Transport	Food and beverages	Other goods and services
Energy	-0.34	-0.11	0.08	0.04
Transport	0.51	-0.42	0.06	0.04
Food and beverages	-0.52	-0.04	-0.50	0.20
Other goods and services	0.35	0.57	0.37	-0.26

	Energy	Transport	Food and beverages	Other goods and services
Energy	-0.34	-0.16	0.05	-0.02
Transport	0.50	-0.59	-0.05	-0.10
Food and beverages	-0.54	-0.29	-0.65	-0.01
Other goods and services	0.27	-0.23	-0.11	-0.93

Table A.9 Between-group uncompensated price elasticities ($\eta_{q_r p_s}$)
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Annex 3 – Within-group elasticity estimates for domestic energy and vehicle fuels

	Energy	Transport
Electricity	0.61	-
Gas	1.35	-
Other fuels	1.44	-
Vehicle fuels	-	0.80

Table A.10 Within-group expenditure elasticities ($\eta^r_{q_i x_r}$)

Table A.11 Within-group compensated price elasticities ($\tilde{\eta}^{r}_{q_{i}p_{j}}$)

	Energy		Transport		
	Electricity	Gas	Other fuels	Vehicle fuels	Other transport
Electricity	-0.29	0.33	0.16	-	-
Gas	0.15	-0.42	0.54	-	-
Other fuels	0.07	0.18	-0.69	-	-
Vehicle fuels	-	-		-0.48	0.14

	Energy		Transport		
	Electricity	Gas	Other fuels	Vehicle fuels	Other transport
Electricity	-0.59	-0.33	-0.55	-	-
Gas	-0.07	-0.91	0.02	-	-
Other fuels	-0.02	-0.01	-0.90	-	-
Vehicle fuels	-	-		-0.66	-0.10

Table A.12 Within-group uncompensated price elasticities ($\eta_{q_i p_j}^r$)

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